

An illustration of a landscape with a brown ground, a blue sky, a green tree, and a small orange figure. A large, light-colored, teardrop-shaped object is positioned above the ground. The text "Sustainable Development" is written in white on a brown background at the bottom.

Sustainable Development

An identical illustration to the one on the left, featuring a landscape with a brown ground, a blue sky, a green tree, and a small orange figure. A large, light-colored, teardrop-shaped object is positioned above the ground. The text "Sustainable Development" is written in white on a brown background at the bottom.

Sustainable Development

Part 8

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**Pollution**

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The EKC and substitution between alternative inputs

- Empirical observations and literature
- The specified model
- A graphical approach

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## The EKC and substitution between alternative inputs

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# Empirical observations and literature

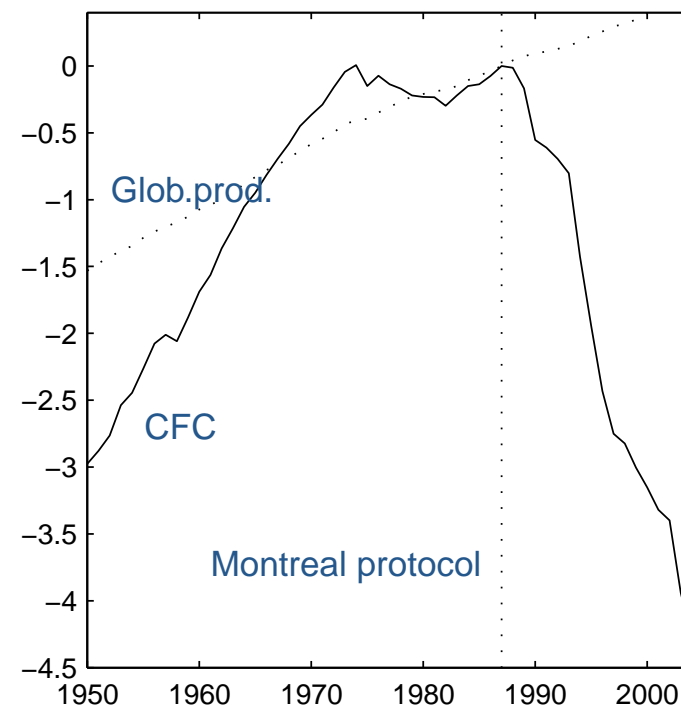
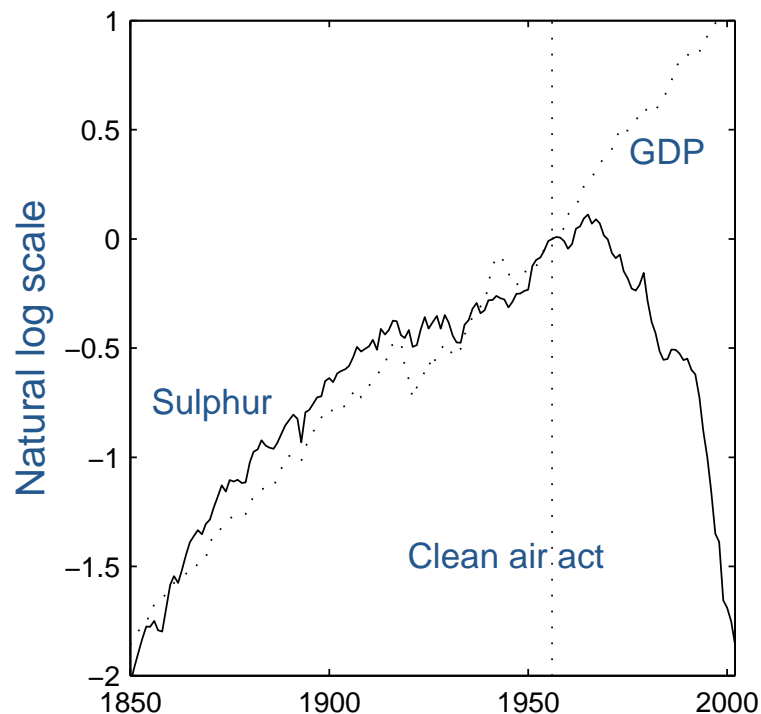
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# Empirical observations and literature

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UK Sulphur emissions compared to total UK GDP, and global CFC production (CFC11+CFC12) compared to total global product.

## Empirical observations and literature

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Grossman and Krueger (1995) is the seminal work.

In the empirically oriented EKC literature there is strong support for the idea that when the flow of a single pollutant in a single country is plotted against time, that flow will in most cases first tend to rise, and later (if enough time has passed) decline. See for instance Grossman and Krueger (1995) and Selden et al. (1999).

However, if we compare paths for the same pollutant across different countries, it is hard to find clear patterns; the turning point is neither at a given time, nor at a given level of per-capita GDP. For instance, Stern (2004) concludes [p1435] that '[t]here is little evidence for a common inverted U-shaped pathway that countries follow as their income rises'.

## Empirical observations and literature

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Despite more than 20 years of research, there is still no widely accepted theoretical explanation for the phenomenon. One reason for this is that researchers building theoretical models have fallen into the trap of treating pollution as an input to production, rather than as a by-product of the use of natural resources, following a tradition going back at least as far as Baumol and Oates (1975).

If we think of pollution as an input in a Cobb–Douglas production function, then we know that the factor share of pollution must be constant. And if we let the marginal damage caused by pollution track income (a natural assumption) then the flow of pollution should be constant as the economy grows. This is like our DHSS-style model with land, in which the price of land tracks the growth rate. Except that here it is the price which is tied to the growth rate, and this leads (endogenously) to a constant flow of pollution.

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When we treat pollution as a by-product of natural-resource use (following Murty et al. (2012)), the analysis changes completely. The social costs of natural resource use are then the sum of extraction costs and the damage costs of the concomitant pollution.

At low income the pollution damages are small and the (constant) extraction cost dominates. And because the natural resource is an input in a Cobb–Douglas production function, natural resource consumption increases with growth, as do polluting emissions.

As income increases, so does the WTP to avoid pollution. The social cost of natural-resource use starts to rise, and resource use levels off. However, more importantly, if there is a cleaner (but more expensive) alternative resource, there will come a point at which this resource is preferred, and pollution falls dramatically.

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## The specified model

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$$Y(t) = [A_L(t)L(t)]^{1-\alpha} R(t)^\alpha e^{-P(t)\phi},$$

$$g = \dot{A}_L(t)/A_L(t) + \dot{L}(t)/L(t),$$

$$R = \sum_{j=1}^n D_j,$$

$$P = \sum_{j=1}^n \psi_j D_j.$$

The cost of a unit of input  $j$  is  $w_j$ .

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$$Y(t) = [A_L(t)L(t)]^{1-\alpha} R(t)^\alpha e^{-P(t)\phi},$$

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$$R = \sum_{j=1}^n D_j,$$

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We can interpret alternative technologies  $j$  and  $k$  simply as alternative resource inputs, for instance low- and high-sulfur coal for electricity generation. However, a third technology  $l$  could be high-sulfur coal combined with flue-gas desulfurization (FGD).

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$$Y(t) = [A_L(t)L(t)]^{1-\alpha} R(t)^\alpha e^{-P(t)\phi},$$

$$g = \dot{A}_L(t)/A_L(t) + \dot{L}(t)/L(t),$$

$$R = \sum_{j=1}^n D_j,$$

$$P = \sum_{j=1}^n \psi_j D_j.$$

If the input is simply a natural resource then we can think of it as being extracted competitively from a large homogeneous stock, with each unit extracted requiring  $w_j$  units of final good as input. But for technology  $l$  the price  $w_l$  would be  $w_k$  plus the unit cost of FGD, and unit emissions  $\psi_l$  would be  $\psi_k \times$  the fraction remaining after FGD.

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$$Y(t) = [A_L(t)L(t)]^{1-\alpha} R(t)^\alpha e^{-P(t)\phi},$$

$$g = \dot{A}_L(t)/A_L(t) + \dot{L}(t)/L(t),$$

$$R = \sum_{j=1}^n D_j,$$

$$P = \sum_{j=1}^n \psi_j D_j.$$

We denote aggregate production net of extraction costs as  $Z$ , so

$$Z = (A_L L)^{1-\alpha} \left( \sum_{j=1}^n D_j \right)^\alpha e^{-(\sum_{j=1}^n \psi_j D_j)\phi} - \sum_{j=1}^n w_j D_j.$$

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Social planner; two technologies.

$$Z = (A_L L)^{1-\alpha} \left( \sum_{j=1}^n D_j \right)^\alpha e^{-(\sum_{j=1}^n \psi_j D_j)^\phi} - \sum_{j=1}^n w_j D_j.$$

$$\text{FOC } D_1 : \alpha Y / (D_1 + D_2) = w_1 + \phi (\psi_1 D_1 + \psi_2 D_2)^{\phi-1} \psi_1 Y.$$

$$\text{And FOC } D_2 : \alpha Y / (D_1 + D_2) = w_2 + \phi (\psi_1 D_1 + \psi_2 D_2)^{\phi-1} \psi_2 Y.$$

MB=MC. Benefits identical, costs differ. Costs: input costs  $w_j$  and damage costs  $\phi P^{\phi-1} \psi_j Y$ .

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Start with the case in which  $w_1 < w_2$  and  $\psi_1 < \psi_2$ , so  $D_1$  is both cheaper and cleaner, and  $D_2$  will never be used.

$$\text{FOC } D_1 : \alpha Y / (D_1 + D_2) = w_1 + \phi (\psi_1 D_1 + \psi_2 D_2)^{\phi-1} \psi_1 Y.$$

When only input  $D_1$  is used, from any given initial state (defined by  $A_L(0)L(0)$ ),  $P$  increases monotonically and approaches a limit of  $\bar{P} = (\alpha/\phi)^{1/\phi}$ . If we let  $A_L(0)L(0)$  approach zero then the initial growth rate of  $P$  approaches  $g$  from below.

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## The specified model

The shadow price of the polluting input to the social planner is the sum of extraction cost and marginal damages. The extraction cost is constant, whereas marginal damages increase linearly in  $Y$ .

So when  $Y$  is small the shadow price is approximately equal to the constant extraction cost, and both resource use and polluting emissions track growth.

As  $Y$  increases, marginal damages increase and hence the shadow price of using the polluting input increases.

When  $Y$  is large marginal damages dominate the extraction cost, the shadow price of using the input grows at the overall growth rate, and emissions (and input use) are constant.

So we have a transition from emissions tracking growth towards (in the limit) constant emissions.

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## The specified model

Now we take the more interesting case when technology 2 is more expensive but clean, i.e.  $\psi_2 = 0$ . In this case, as  $Y$  increases, the increasing importance of pollution damages does not just lead to pollution abatement within technology 1 —i.e. the substitution of labour–capital for  $D_1$  in production—it also narrows the gap between the social costs of  $D_1$  (cheap and dirty) and  $D_2$  (expensive but cleaner). At some point the social costs are equal, and a transition to the cleaner technology begins.

From this point on the transition is gradual, because marginal damages decrease as emissions decrease (as long as  $\phi > 1$ ).

$$\alpha Y / (D_1 + D_2) = w_1 + \phi (\psi_1 D_1 + \psi_2 D_2)^{\phi-1} \psi_1 Y.$$

$$\alpha Y / (D_1 + D_2) = w_2 + \phi (\psi_1 D_1 + \psi_2 D_2)^{\phi-1} \psi_2 Y.$$

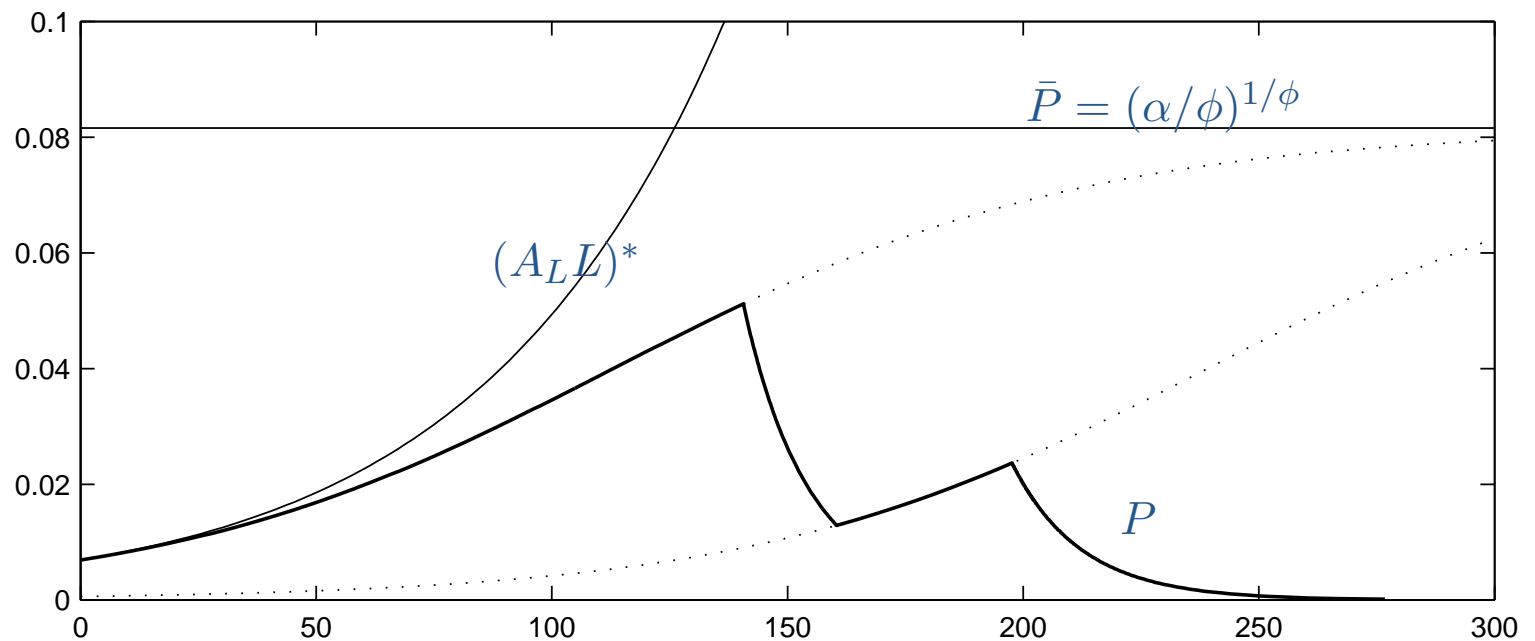


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In the figure we illustrate the development of the economy in a specific case with three technologies, the third of which is perfectly clean. The dotted lines show the paths of  $P$  which would be followed if (respectively) only technologies 1 and 2 were available.



# A graphical approach

The EKC and substitution between alternative inputs

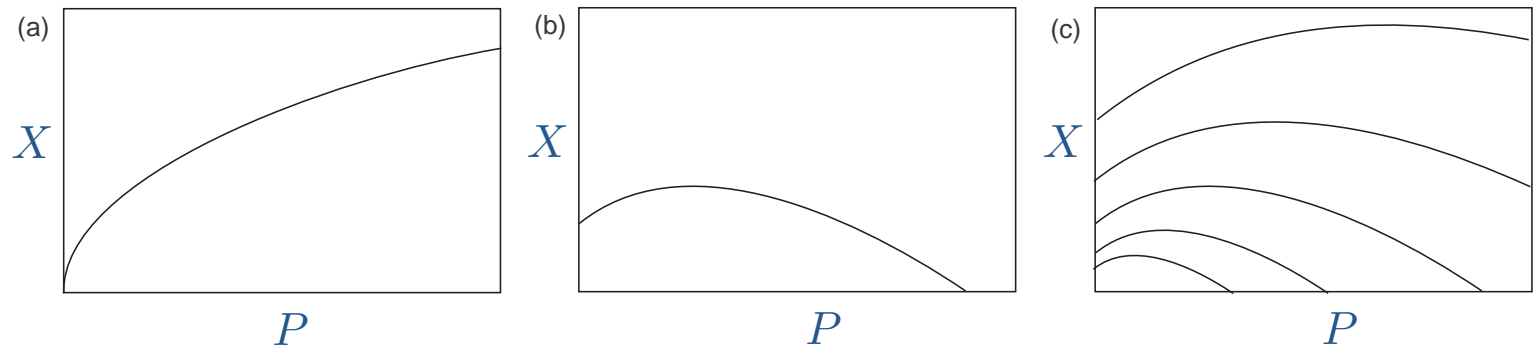
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## A graphical approach

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PPFs over production and pollution.



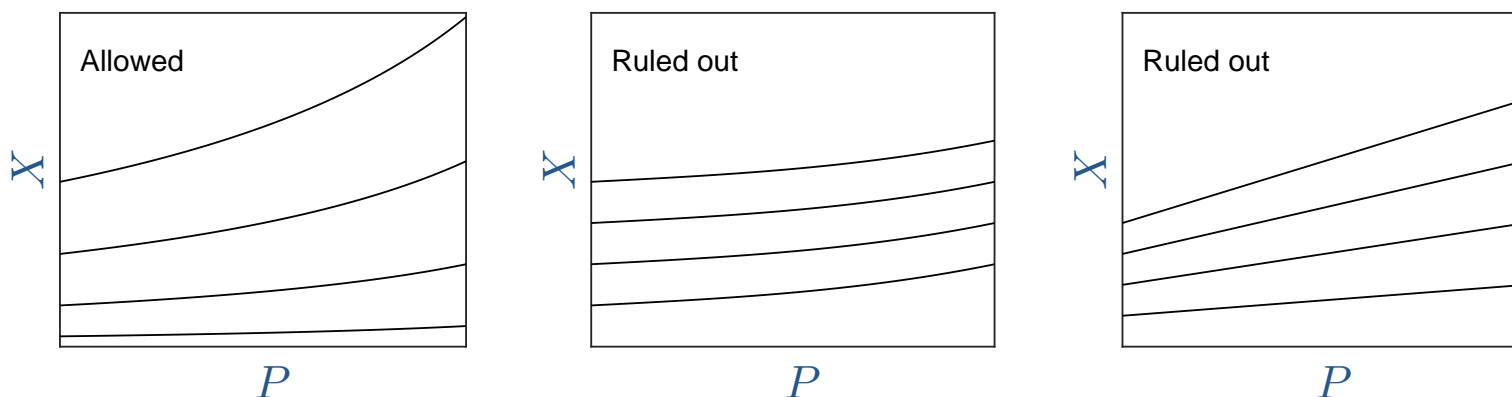
PPFs. The PPF in (a) is not allowed because there is no turning point; the PPF in (b) is allowed; in (c) we see a set of PPFs for different productivity levels.

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Indifference curves over production and pollution.

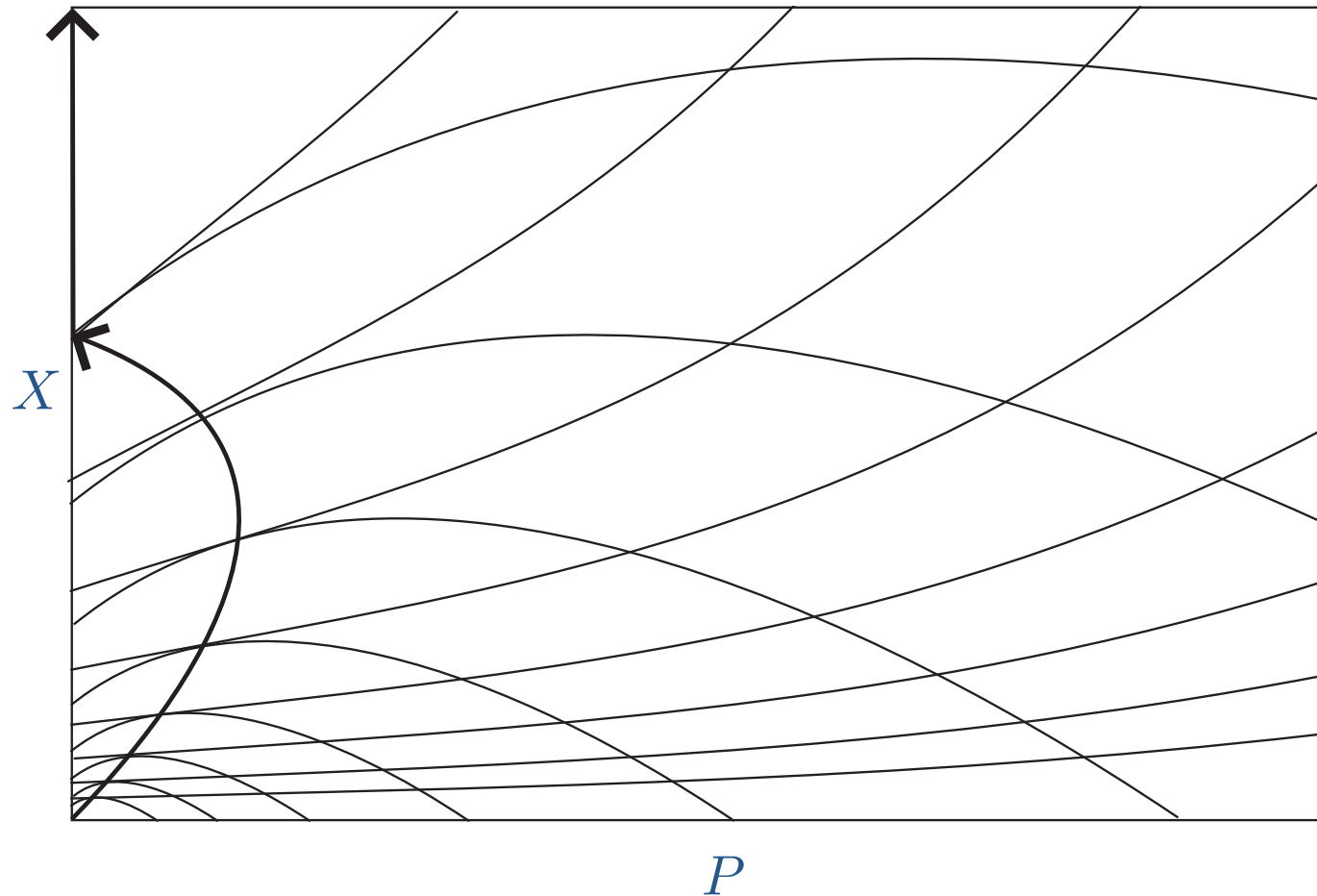


Three sets of indifference curves. The second is ruled out because  $dX/dP$  does not increase in  $X$ , implying that the WTP to remove a unit of pollution does not increase in income, and the third is ruled out because the curves are not strictly convex.

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The rise and fall of  $P$  as productivity increases.

# Conclusions

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Does the model make sense, have explanatory power?

Discuss cases! What should be added?

Climate??